

## From yesterday, section 3.2:

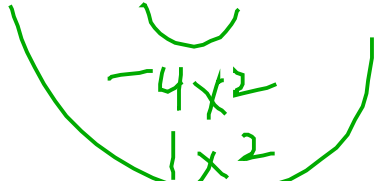
11.  $R(x) = -x^5 + 5x^3 - 4x$

$$= -x(x^4 - 5x^2 + 4)$$

$$= -x(x^2 - 4)(x^2 - 1)$$

$$= -x(x+2)(x-2)(x+1)(x-1)$$

43.  $P(x) = x^4 - 3x^2 - 4$

$$= (x^2 - 4)(x^2 + 1)$$


$$0 = (x+2)(x-2)(x^2+1)$$

$$x = -2 \quad x = 2$$

## 3.3 Notes: Dividing Polynomials

$$2x^3 - 7x^2 + 5 \div x - 3$$

Be sure to account for  
all possible exponents!!

rewrite :  $x - 3 \overline{) 2x^3 - 7x^2 + 0x + 5}$

Use parentheses  
when subtracting!!

# 3.3 Notes: Dividing Polynomials

$$\underline{2x^3 - 7x^2 + 5} \div x - 3$$

$$\boxed{r - 4}$$

Be sure to account for all possible exponents!!

$$2x^2 - x - 3$$

rewrite :

$$x - 3 \overline{) 2x^3 - 7x^2 + 0x + 5}$$

$$\underline{-(2x^3 - 6x^2)}$$

$$\underline{-( -x^2 + 3x )}$$

$$\underline{-( -3x + 9 )}$$

$$\boxed{-4}$$

Use parentheses when subtracting!!

# 3.3 Notes: Synthetic Division

*(an alternative to dividing polynomials)*

$$2x^3 - 7x^2 + 5 \div x - 3$$

rewrite:  $x - 3 \overline{) 2x^3 - 7x^2 + 0x + 5}$

or rewrite:

<u>3</u>		2	-7	0	5	
		↓	6	-3	-9	add
		2	-1	-3	-4	
		quotient			remainder	

*multiply* (green arrow from 3 to 2)  
*add* (red arrows from 6 to -7, -3 to 0, -9 to 5)

Synthetic division:  
see video in ebook  
for more details

$2x^2 - x - 3$ remainder $-4$
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### Long Division

$$\begin{array}{r} 2x^2 - x - 3 \\ x - 3 \overline{) 2x^3 - 7x^2 + 0x + 5} \\ \underline{2x^3 - 6x^2} \phantom{+ 0x + 5} \\ -x^2 + 0x \phantom{+ 5} \\ \underline{-x^2 + 3x} \phantom{+ 5} \\ -3x + 5 \\ \underline{-3x + 9} \\ -4 \end{array}$$

Quotient:  $2x^2 - x - 3$

Remainder:  $-4$

### Synthetic Division

$$\begin{array}{r|rrrr} 3 & 2 & -7 & 0 & 5 \\ & 6 & -3 & -9 & \\ \hline & 2 & -1 & -3 & -4 \end{array}$$

Quotient:  $2x^2 - x - 3$

Remainder:  $-4$

For #16,29,31, please be sure to solve for the quotient and remainder using LONG DIVISION and SYNTHETIC DIVISION.

16. Find the quotient and the remainder using  
LONG DIVISION and SYNTHETIC DIVISION.

$$\frac{x^3 + 2x^2 - x + 1}{x + 3}$$

$x^2 - x + 2$

$$\begin{array}{r} (x+3) \overline{) x^3 + 2x^2 - x + 1} \\ \underline{-(x^3 + 3x^2)} \phantom{-x + 1} \\ -x^2 - x + 1 \\ \underline{-(-x^2 - 3x)} \phantom{+ 1} \\ 2x + 1 \\ \underline{-(2x + 6)} \\ -5 \end{array}$$

62. FACTOR THEOREM: Show that the given value(s) of  $c$  are zeros of  $P(x)$ , and find all other zeros of  $P(x)$

$$2x^4 - 13x^3 + 7x^2 + 37x + 15, \quad c = -1, 3$$

$$\begin{array}{r} \underline{-1} \mid 2 \quad -13 \quad 7 \quad 37 \quad 15 \\ \quad \downarrow -2 \quad 15 \quad -22 \quad -15 \\ \hline 3 \mid 2 \quad -15 \quad 22 \quad 15 \quad \boxed{0} \\ \quad \downarrow 6 \quad -27 \quad -15 \\ \hline 2 \quad -9 \quad -5 \quad \boxed{0} \end{array}$$